



MS – 319

VI Semester B.A./B.Sc. Examination, May 2016
(Semester Scheme) (NS) (F + R)
(2013 – 14 and Onwards)
MATHEMATICS – VIII

Time : 3 Hours

Max. Marks : 100

Instruction: Answer all questions.

I. Answer any fifteen questions : (15×2=30)

- 1) Find the kinetic energy of the particle of mass 10 units moving with velocity $2\hat{i} - 3\hat{j} + 4\hat{k}$.
- 2) In a simple harmonic motion, if 'f' is the acceleration, 'v' the velocity at any instant and 'T' is the period, show that $f^2 T^2 + 4\pi^2 v^2$ is a constant.
- 3) Find the maximum horizontal range when the velocity of projection is 14 mtrs/sec.
- 4) Write the condition for the particle to strike the inclined plane at right angles.
- 5) A point describes the cycloid $s = 4a \sin(\psi)$ with uniform speed, show that its acceleration at any point is $\frac{v^2}{\sqrt{16a^2 - s^2}}$.
- 6) A particle moves along a curve so that its tangential and normal acceleration are equal. Find its velocity.
- 7) Write the expressions for radial acceleration and transverse acceleration.
- 8) Define apsidal distance.

9) If $I = \int_{x_1}^{x_2} f(x, y, y') dx$ then prove that $\delta \int_{x_1}^{x_2} f(x, y, y') dx = \int_{x_1}^{x_2} \delta f(x, y, y') dx$.

10) State Euler's equation.

11) Define geodesic on a curve.

12) Find the differential equation of the functional $I = \int_0^{\pi/2} [y^2 - (y')^2 - 2y \sin x] dx$.

P.T.O.



- 13) Use bisection method in two stages to obtain the root of the equation
 $x^3 - 2x - 5 = 0$.
- 14) Find the real root of the equation $x^3 - 2x - 5 = 0$ by Regula-Falsi method (Only First approximate value).
- 15) Find the real root of the equation $x^4 - x - 10 = 0$ which is near to $x = 2$ by Newton-Raphson method (only two approximate values).
- 16) Solve the system of equations
 $x + y + 5z = 110$
 $27x + 6y - z = 85$
 $6x + 15y + 2z = 72$
 by Gauss-Seidal method (only one set of solution).
- 17) Using Euler's method, solve
 $\frac{dy}{dx} = x + y$, $y(0) = 1$ for $x = 0.0$ (0.2) 1.0 (only two approximate values).
- 18) Find the order and degree of the difference equation $y_{x+2} - 7y_{x+1} + 2y_x = 0$.
- 19) Form the difference equation by eliminating 'a' from the relation $y_n = a \cdot 3^n$.
- 20) Solve $y_{x+2} - 2y_{x+1} + y_x = 0$ by the method of differences.

II. Answer any three of the following :

(3x5=15)

- 1) Show that $\vec{F} = (y^2 z^3 - 6xz^2) \hat{i} + 2xyz^3 \hat{j} + (3xy^2 z^2 - 6x^2 z) \hat{k}$ is a conservative force field. Find the work done by \vec{F} in moving a particle from $(-2, 1, 3)$ to $(1, -2, -1)$.
- 2) A particle executing simple harmonic motion along a line, travels a distance 'a' in the first second after starting from rest and in the next second it travels a distance 'b'. Show that the amplitude of the motion is $\frac{2a^2}{3a-b}$.
- 3) If 'R' be the range of a projectile on the horizontal plane and 'h' its maximum height for a given angle of projection. Show that the maximum horizontal range with the same velocity of projection is $\left[2h + \frac{R^2}{8h} \right]$.
- 4) A particle is projected with velocity 80 ft/sec. at an angle of 45° to the horizontal. Find its range on the plane inclined at an angle of 30° to the horizontal when projected up to the plane.

III. Answer any two of the following :

(2×5=10)

- 1) Derive the expression for radial and transverse velocity.
- 2) A particle describes the curve $2r = a(1 + \cos \theta)$ under the central force towards the pole. Find the law of force.
- 3) Derive the expression for the velocity of the particle at any point on the central orbit in the form $v^2 = h^2 \left[\left(\frac{du}{d\theta} \right)^2 + u^2 \right]$.
- 4) The component of velocity of a particle moving along a plane curve along and perpendicular to the radius vector to a fixed point are λr^n and $\mu \theta^n$ respectively, where λ and μ are constants. Derive the equation of the curve.

IV. Answer any three of the following :

(3×5=15)

- 1) Find the extremal of the functional $I = \int_1^2 \left[\frac{\sqrt{1+(y')^2}}{x} \right] dx$ given $y(1) = 0$ and $y(2) = 1$.
- 2) Show that the general solution of Euler's equation for the integral $\int_a^b \frac{1}{y} \left[\sqrt{1+(y')^2} \right] dx$ is $(x - B)^2 + y^2 = R^2$.
- 3) Show that the geodesics on a right circular cylinder is a circular helix.
- 4) Show that extremal of the functional $\int_0^2 \left[\sqrt{1+(y')^2} \right] dx$ subject to the constraint $\int_0^2 y dx = \frac{\pi}{2}$ and end conditions $y(0) = 0, y(2) = 2$ is a circular arc.

V. Answer any three of the following :

(3×5=15)

- 1) Using bisection method find the real root of the equation $x^3 - 5x + 3 = 0$ lying between 0 and 1 correct to 3 places of decimals.
- 2) Solve the equation $x^3 - 4x + 1 = 0$ over (0, 1) by Regula-Falsi method.



3) Solve the equations $20x + y - 2z = 17$; $3x + 20y - z = -18$;
 $2x - 3y + 20z = 25$ by Jacobi iteration method.

4) Find the largest eigen value of the matrix $\begin{pmatrix} -4 & -5 \\ 1 & 2 \end{pmatrix}$ by power method.

VI. Answer **any three** of the following :

(3x5=15)

1) Use Taylor's series method to find y at $x = 0.1$ considering terms upto third degree terms given $\frac{dy}{dx} = x^2 + y^2$ and $y(0) = 1$.

2) Solve $\frac{dy}{dx} = x + y$, $y(0) = 1$ for $x = 0.025$ by Picard's method upto 3rd approximation.

3) Solve $\frac{dy}{dx} = xy$; $y(1) = 2$, find the approximate solution at $x = 1.2$ using Runge-Kutta method.

OR

Form the difference equation by eliminating the arbitrary constants 'a' and 'b'
 $y_x = a.2^x + b.3^x$.

4) Solve the difference equation $(E^2 - 8E + 15)y_n = 3^n + e^{3n}$.
